

Composite-pulse magnetometry with a solid-state quantum sensor

Clarice D. Aiello, Masashi Hirose, and Paola Cappellaro*

*Department of Nuclear Science and Engineering,
Massachusetts Institute of Technology, Cambridge, MA 02139, USA*

(Dated: November 30, 2012)

The sensitivity of quantum magnetometers is challenged by control errors and, especially in the solid-state, by their short coherence times. Refocusing techniques can overcome these limitations and improve the sensitivity to periodic fields, but they come at the cost of reduced bandwidth and cannot be applied to sense static or aperiodic fields. Here we experimentally demonstrate that continuous driving of the sensor spin by a composite pulse known as rotary-echo yields a flexible magnetometry scheme, mitigating both driving power imperfections and decoherence. A suitable choice of rotary-echo parameters compensates for different scenarios of noise strength and origin. The method can be applied to nanoscale sensing in variable environments or to realize noise spectroscopy. In a room-temperature implementation based on a single electronic spin in diamond, composite-pulse magnetometry provides a tunable trade-off between sensitivities in the $\mu\text{THz}^{-\frac{1}{2}}$ range, comparable to those obtained with Ramsey spectroscopy, and coherence times approaching T_1 .

INTRODUCTION

Solid-state quantum sensors attract much attention given their potential for high sensitivity and nano applications. In particular, the electronic spin of the nitrogen-vacancy (NV) color center in diamond is a robust quantum sensor [1–3] due to a combination of highly desirable properties: optical initialization and read-out, long coherence times at room temperature ($T_1 > 2$ ms [4, 5], $T_2 \gtrsim 0.5$ ms [6]), the potential to harness the surrounding spin bath for memory and sensitivity enhancement [7, 8], and bio-compatibility [9].

Magnetometry schemes based on quantum spin probes (qubits) usually measure the detuning $\delta\omega$ from a known resonance. The most widely used method is Ramsey spectroscopy [10], which measures the relative phase $\delta\omega t$ the qubit acquires when evolving freely after preparation in a superposition state. In the solid state, a severe drawback of this scheme is the short free-evolution dephasing time, T_2^* , which limits the interrogation time. Dynamical decoupling (DD) techniques such as Hahn-echo [11] or Carr-Purcell-Meiboom-Gill [12] sequences can extend the coherence time. Unfortunately, such schemes also refocus the effects of static magnetic fields and are thus not applicable for DC-magnetometry. Even if $\delta\omega$ oscillates with a known frequency (AC-magnetometry), DD schemes impose severe restrictions on the bandwidth, as the optimal sensitivity is reached only if the field period matches the DD cycle time [1]. Schemes based on continuous driving are thus of special interest for metrology in the solid-state because they can lead to extended coherence times [13]. Recently, DC-magnetometry based on Rabi frequency beats was demonstrated [14]; in that method, a small detuning along the static magnetic field produces a shift $\approx \frac{\delta\omega^2}{2\Omega}$ of the bare Rabi frequency Ω . Despite ideally allowing for interrogation times approaching T_1 , limiting factors such as noise in the driving field [14] and the bad scaling in $\delta\omega \ll \Omega$ make Rabi-beat magnetometry unattractive. More complex driving modulations [15] can provide not only a better refocusing of driving field inhomogeneities, but also different scalings with $\delta\omega$, yielding improved magnetometry. In this work, we use a novel composite-pulse magnetometry method as a means of both extending coherence times as expected by continuous excitation, and keeping a good scaling with $\delta\omega$, which increases sensitivity. The ϑ -rotary-echo (RE) is a simple composite pulse (Fig. 1.a) designed to correct for inhomogeneities in the excitation field [16]; here, ϑ parametrizes the rotation angle of the half-echo pulse. For $\vartheta \neq 2\pi k$, $k \in \mathbb{Z}$, RE does not refocus magnetic fields along the qubit quantization axes and can therefore be used for DC-magnetometry. For $\vartheta = 2\pi k$, RE provides superior decoupling from both dephasing [17–19] and microwave noise and can be used to achieve AC-magnetometry [20].

* pcappell@mit.edu

RESULTS

Dynamics under rotary-echo sequence

In the rotating frame associated with the microwave field, and applying the rotating wave approximation, the Hamiltonian describing a continuous stream of ϑ -REs is

$$\mathcal{H}(t) = \frac{1}{2} [\Omega \text{SW}(t) \sigma_x + \delta\omega (\mathbb{1} - \sigma_z)],$$

where $\text{SW}(t) = \pm 1$ is the square wave of period $T = \frac{2\vartheta}{\Omega}$. On resonance ($\delta\omega = 0$) the evolution is governed by the propagator $U_0 = e^{i\frac{\Omega}{2}\text{TW}(t)\sigma_x}$, with $\text{TW}(t)$ the triangular wave representing the integral of $\text{SW}(t)$. We approximate the time evolution in the presence of a detuning $\delta\omega$ by a first order Average Hamiltonian expansion [21], yielding an effective Hamiltonian over the cycle (Supplementary Methods, ‘Dynamics under rotary-echo sequence’),

$$\overline{\mathcal{H}}^{(1)} = -\frac{\delta\omega}{\vartheta} \sin\left(\frac{\vartheta}{2}\right) \left[\cos\left(\frac{\vartheta}{2}\right) \sigma_z - \sin\left(\frac{\vartheta}{2}\right) \sigma_y \right].$$

Extending the above approximation to include the fast Rabi-like oscillations of frequency $\frac{\pi\Omega}{(\vartheta \bmod 2\pi)}$, we can thus calculate the population evolution for one of the qubit states,

$$\mathcal{S}(t) \approx \frac{1}{2} \left[1 + \cos^2\left(\frac{\vartheta}{2}\right) + \sin^2\left(\frac{\vartheta}{2}\right) \cos\left(\frac{2\delta\omega t}{\vartheta} \sin\left(\frac{\vartheta}{2}\right)\right) \cos\left(\frac{\pi\Omega t}{(\vartheta \bmod 2\pi)}\right) \right], \quad (1)$$

The signal \mathcal{S} reveals the presence of two spectral lines at $\frac{\pi\Omega}{(\vartheta \bmod 2\pi)} \pm \frac{2\delta\omega}{\vartheta} \sin\left(\frac{\vartheta}{2}\right)$ for a detuning $\delta\omega$.

Sensitivity of the method

Thanks to the linear dependence on $\delta\omega$, we expect a favorable scaling of the sensitivity η , given by the shot-noise-limited magnetic field resolution per unit measurement time [1, 22]. For N measurements and a signal standard deviation $\Delta\mathcal{S}$, the sensitivity is

$$\eta = \Delta B \sqrt{\mathcal{T}} = \frac{1}{\gamma_e} \lim_{\delta\omega \rightarrow 0} \frac{\Delta\mathcal{S}}{\left| \frac{\partial \mathcal{S}}{\partial \delta\omega} \right|} \sqrt{N(t + t_d)}, \quad (2)$$

where γ_e ($\approx 2.8\text{MHzG}^{-1}$ for NV) is the sensor gyromagnetic ratio and ΔB is the minimum detectable field. We broke down the total measurement time \mathcal{T} into interrogation time t and the dead-time t_d required for initialization and readout. In the absence of relaxation, and neglecting t_d , a RE magnetometer interrogated at complete echo cycles $t = n\frac{2\vartheta}{\Omega}$ yields $\eta_{\text{RE}} = \frac{1}{\gamma_e \sqrt{t}} \frac{\vartheta}{2 \sin^2(\vartheta/2)}$. As shown in Fig. 1.b, RE magnetometry has thus sensitivities comparable to Ramsey spectroscopy, $\eta_{\text{Ram}} \approx \frac{1}{\gamma_e \sqrt{t}}$. Conversely, Rabi-beat magnetometry has $\eta_{\text{Rabi}} \approx \frac{\sqrt{2\Omega}}{\gamma_e}$ at large times (Supplementary Methods, ‘Rabi-beat magnetometry’), which makes it unsuitable for magnetometry despite long coherence times.

To establish the sensitivity limits of RE magnetometry and compare them to other DC-magnetometry strategies, we carried out proof-of-principle experiments in single NV centers in a bulk electronic-grade diamond sample. A static magnetic field $B_{\parallel} \approx 100$ G effectively singles out a qubit $\{|0\rangle, |1\rangle\}$ from the NV ground-state spin triplet, as the Zeeman shift lifts the degeneracy between the $|\pm 1\rangle$ levels. The qubit is coupled to the spin-1 ^{14}N nucleus that composes the defect by an isotropic hyperfine interaction of strength $A \approx 2\pi \times 2.17\text{MHz}$. After optical polarization into state $|0\rangle$, we apply a stream of n RE cycles using microwaves with frequency ω close to the qubit resonance $\omega_0 = \Delta + \gamma_e B_{\parallel}$, where $\Delta = 2.87\text{GHz}$ is the NV zero-field splitting. Because of the hyperfine coupling, ω_0 is the resonance frequency only when the nuclear state is $m_{\text{I}} = 0$. At room temperature, the nitrogen nucleus is unpolarized and, while its state does not change over one experimental run, in the course of the $N \sim 10^6$ experimental realizations, $\approx 2/3$ of the times the qubit is off-resonantly driven by $|\delta\omega| = A$. A typical n -cycle RE fluorescence signal is plotted in Fig. 1.c for $\vartheta = \pi$ and $\Omega \approx 2\pi \times 17\text{MHz}$, while to determine the frequency content of the signal we plot the periodogram

(Supplementary Methods, ‘Periodogram’) in Fig. 2.

The number of distinguishable frequencies increases with interrogation time at the expense of signal-to-noise ratio. RE-magnetometry not only discriminates the frequency shifts due to $A \approx 2\pi \times (2.14 \pm 0.03)\text{MHz}$ but, for interrogation times as short as $5\mu\text{s}$, also those due to a small residual detuning $b \approx 2\pi \times (0.17 \pm 0.02)\text{MHz}$ from the presumed resonance. In contrast, under the same experimental conditions, Rabi magnetometry does not discern such a detuning before an interrogation time $\approx 188\mu\text{s}$ (Supplementary Methods, ‘Rabi-beat magnetometry’, and Supplementary Fig. S1). With longer interrogation times $\sim 15\mu\text{s}$ as in Fig. 2.b (also in Supplementary Fig. S2), we can detect a frequency as small as $b \approx 2\pi \times (64 \pm 12)\text{kHz}$.

To determine the experimental sensitivities, we estimate $|\frac{\partial S}{\partial \delta\omega}|$ by driving the qubit with varying ω , at fixed interrogation times t (Fig. 3.a). For each t , in Fig. 3.b we plot the minimum $\frac{1}{\gamma_e} \frac{\Delta S}{|\frac{\partial S}{\partial \delta\omega}|} \sqrt{Nt}$ and compare it to the adjusted theoretical sensitivity $\eta/(C \times C_A)$. Here, $(C \times C_A) \approx (5.9 \pm 1.4) \times 10^{-3}$ in our setup, is a factor taking into account readout inefficiencies and a correction for the presence of the hyperfine interaction [1] (also Supplementary Methods, ‘Experimental sensitivity’). The sensitivities agree with the theoretical model, with optimal $\sim 10\mu\text{THz}^{-\frac{1}{2}}$, which is within the range of sensitivities achieved with other magnetometry schemes alternative to Ramsey [23, 24], and with the added flexibility made possible by a suitable choice of RE rotation angle. Improved sensitivities are expected from isotopically pure diamond [25]; an adequate choice of interrogation times or polarization of the nuclear spin can easily set $C_A = 1$, while C can be improved by efficient photon collection [26] or using repeated readout methods [27].

Effect of noise

The sensitivity of a NV magnetometer is ultimately limited by the interaction of the quantum probe with the nuclear spin bath. We model the effect of the spin bath by a classical noise source along σ_z [28], described by an Ornstein-Uhlenbeck (OU) process of strength σ and correlation time τ_c . In the limit of long τ_c (static bath), the dephasing time associated with RE (Ramsey) magnetometry is $T'_{\text{RE}} = \frac{\vartheta}{\sigma\sqrt{2}|\sin(\vartheta/2)|}$ ($T_2^* = T'_{\text{Ram}} = \frac{\sqrt{2}}{\sigma}$) respectively (for the general case, see Supplementary Methods, ‘Evolution under bath noise’, and Supplementary Fig. S5.a). While at the optimum interrogation time $\frac{T'}{2}$ one has $\eta_{\text{RE}}/\eta_{\text{Ram}} = \sqrt{\frac{\vartheta}{2\sin(\vartheta/2)^3}} > 1$, RE magnetometry allows a greater flexibility in choosing the effective coherence time, as larger ϑ increase the resilience to bath noise. Thus one can match the RE interrogation time to the duration of the field one wants to measure.

In addition, RE can yield an overall advantage when taking into consideration the dead-time t_d . If $t_d \gg T'_{\text{Ram}}$, as in repeated readout methods [27], a gain in sensitivity can be reached by exploiting the longer interrogation times enabled by RE magnetometry (Supplementary Methods, ‘Repeated readouts’, and Supplementary Fig. S6). An even larger advantage is given by AC-magnetometry with $2\pi k$ -RE [20], since RE provides better protection than pulsed DD schemes [17, 20].

Excitation field instabilities along σ_x also accelerate the decay of RE and Rabi signals. However, provided the echo period is shorter than τ_c , RE magnetometry corrects for stochastic noise in Rabi frequency (Supplementary Methods, ‘Evolution under excitation field noise’, and Supplementary Fig. S5.b). This protection was demonstrated experimentally by applying static and OU noise ($\tau_c \approx 200\text{ns}$) in the excitation microwave, both with strength 0.05Ω . The results for Rabi and $\vartheta = \{\pi, 5\pi\}$ -RE sequences in Fig. 4 clearly show that whereas the Rabi signal decays within $\approx 0.5\mu\text{s}$, 5π -RE refocuses static excitation noise and presents only a very weak decay under finite-correlation noise after much longer interrogation times $\approx 3\mu\text{s}$, in agreement with the theoretical prediction; π -RE is robust against the same noise profiles.

DISCUSSION

The unique ability of the RE magnetometer to adjust its response to distinct noise sources is relevant when the sample producing the magnetic field of interest is immersed in a realistic environment; moreover, the field source might itself have a finite duration or duty cycle. Most experimentally relevant fields, such as those arising from biological samples, might last only for a finite amount of time, when triggered, or be slowly varying so that one can only record their time-average. Thus, it becomes interesting to be able to tune the interrogation time in order to capture and average over the complete physical process. The advantage is two-fold: the protection from noise can be tuned by changing the echo angle, thus allowing the interrogation times to be varied. Techniques for repeated readout in the presence of a strong magnetic field $\gtrsim 1000\text{G}$ [27] (also Supplementary Methods, ‘Repeated readouts’) can at once improve sensitivities and enable the use of much lower qubit resonance frequencies $\sim\text{MHz}$, preferable in biological settings.

Additionally, a RE-magnetometer can discriminate magnetic noise sources given the sensor’s well-understood decoherence behavior under different noise profiles, effectively enabling noise spectroscopy for both σ_z and σ_x -type noises.

NV center-based RE magnetometry could find useful application, for example, to sense the activity of differently-sized calcium signaling domains in living cells, more specifically in neurons. Transient calcium fluxes regulate a myriad of cell reactions [29]. The signaling specificity of such fluxes is determined by their duration and mean travelled distance between membrane channel and cytoplasm receptor. The smaller, faster-signaling domains have resisted thorough investigation via both diffraction-limited optical microscopy [29], and the use of fluorescing dyes, which do not respond fast or accurately enough to Ca^{2+} transients [30]. The magnetic field produced by as few as 10^5 Ca^{2+} , being diffused within $\sim 10\mu\text{s}$ through a $\sim 200\text{nm}$ domain, can be picked up by a nanodiamond scanning sensor [31, 32] with sensitivity $\sim 10\mu\text{THz}^{-\frac{1}{2}}$ placed at close proximity $\sim 10\text{nm}$ (Supplementary Methods, ‘Calcium signaling domains’). The trade-off between sensitivity and optimal interrogation time under RE magnetometry can be optimized to the characteristics of the signaling domain under study by a suitable choice of ϑ .

In conclusion, we have demonstrated a quantum magnetometry scheme based on composite-pulses. Its key interest stems both from the continuous-excitation character, offering superior performance for solid state sensors such as the NV center, and from the possibility of tuning the sensor’s coherence time and sensitivity in the presence of variable or unknown sensing environments, to protect from or map noise sources. Current technology enables immediate implementation of such scheme at the nanoscale.

METHODS

Quantum magnetometer description

The NV center is a naturally occurring point defect in diamond, composed of a vacancy adjacent to a substitutional nitrogen in the carbon lattice. The ground state of the negatively charged NV center is a spin-triplet with zero-field splitting $\Delta = 2.87\text{GHz}$ between the $m_S = 0$ and $m_S = \pm 1$ sub-levels. Coherent optical excitation at 532nm promotes the quantum state of the defect non-resonantly to the first orbital excited state. While the $m_S = 0$ state mostly relaxes with phonon-mediated fluorescent emission ($\approx 650 - 800\text{nm}$), the $m_S = \pm 1$ states have in addition an alternative, non-radiative decay mode to the $m_S = 0$ state via metastable singlet states. Due to this property, each ground state is distinguishable by monitoring the intensity of emitted photons during a short pulse of optical excitation. Additionally, continuous optical excitation polarizes the NV into the $m_S = 0$ state. We apply a magnetic field ($\approx 100\text{G}$) along a crystal axis $\langle 111 \rangle$ to lift the degeneracy between the $m_S = \pm 1$ states and drive an effective two-level system $m_S = \{0, 1\}$ at the resonant frequency ($\omega_0 \approx 3.15\text{GHz}$) obtained by continuous wave electron spin resonance and Ramsey fringe experiments.

Experimental setup description

Experiments were run at room-temperature with single NV centers from an electronic grade single crystal plate ($[100]$ orientation, Element 6) with a substitutional nitrogen concentration < 5 ppb. The fluorescence of single NV centers is identified by a home-built confocal scanning microscope. The sample is mounted on a piezo stage (Nano-3D200, Mad City Labs). The excitation at 532nm is provided by a diode-pumped laser (Coherent Compass 315M), and fluorescence in the phonon sideband ($\sim 650 - 800\text{nm}$) is collected by a 100x, NA = 1.3 oil immersion objective (Nikon Plan Fluor). The fluorescence photons are collected into a single-mode broadband fiber of NA = 0.12 (Font Canada) and sent to a single-photon counting module (SPCM-AQRH-13-FC, Perkin Elmer) with acquisition time 100 or 200 ns.

Laser pulses for polarization and detection are generated by an acousto-optic modulator with rise time $\lesssim 7\text{ns}$ (1250C-848, Isomet). A signal generator (N5183A-520, Agilent) provides microwave fields to coherently manipulate the qubit. An arbitrary waveform generator at 1.2GS/s (AWG5014B, Tektronix) is employed to shape microwave pulses with the help of an I/Q mixer (IQ-0318L, Marki Microwave), and to time the whole experimental sequence. Microwaves are amplified (GT-1000A, Gigatronix) and subsequently delivered to the sample by a copper microstrip mounted on a printed circuit board, fabricated in MACOR to reduce losses.

A static magnetic field is applied by a permanent magnet (BX0X0X0-N52, K&J Magnetics) mounted on a rotation stage, which at its turn is attached to a three-axis translation stage; this arrangement enables the adjustment of the magnetic field angle with respect to the sample. The magnetic field is aligned along a $[111]$ axis by maximizing the Zeeman splitting in a CW ESR spectrum.

In each experimental run, we normalize the signal with respect to the reference counts from the $m_S = \{0, 1\}$ states, where the transfer to state $m_S = 1$ is done by adiabatic passage.

REFERENCES

- [1] J. M. Taylor, P. Cappellaro, L. Childress, L. Jiang, D. Budker, P. R. Hemmer, A. Yacoby, R. Walsworth, and M. D. Lukin, *High-sensitivity diamond magnetometer with nanoscale resolution*. *Nature Phys.* **4**, 810–816 (2008)
- [2] J. R. Maze, P. L. Stanwix, J. S. Hodges, S. Hong, J. M. Taylor, P. Cappellaro, L. Jiang, A. Zibrov, A. Yacoby, R. Walsworth, and M. D. Lukin, *Nanoscale magnetic sensing with an individual electronic spin qubit in diamond*. *Nature* **455**, 644–647 (2008)
- [3] G. Balasubramanian, I.-Y. Chan, R. Kolesov, M. Al-Hmoud, C. Shin, C. Kim, A. Wojcik, P. R. Hemmer, A. Krüger, F. Jelezko, and J. Wrachtrup, *Magnetic resonance imaging and scanning probe magnetometry with single spins under ambient conditions*. *Nature* **445**, 648–651 (2008)
- [4] A. Jarmola, V. M. Acosta, K. Jensen, S. Chemerisov, and D. Budker, *Temperature- and magnetic-field-dependent longitudinal spin relaxation in nitrogen-vacancy ensembles in diamond*. *Phys. Rev. Lett.* **108**, 197601 (2012)
- [5] G. Waldherr, J. Beck, P. Neumann, R. Said, M. Nitsche, M. Markham, D. J. Twitchen, J. Twamley, F. Jelezko, and J. Wrachtrup, *High-dynamic-range magnetometry with a single nuclear spin in diamond*. *Nature Nanotech.* **7**, 105–108 (2012)
- [6] L. Childress, M. V. Gurudev Dutt, J. M. Taylor, A. S. Zibrov, F. Jelezko, J. Wrachtrup, P. R. Hemmer, and M. D. Lukin, *Coherent dynamics of coupled electron and nuclear spin qubits in diamond*. *Science* **314**, 281–285 (2006)
- [7] P. Cappellaro, G. Goldstein, J. S. Hodges, L. Jiang, J. R. Maze, A. S. Sørensen, and M. D. Lukin, *Environment-assisted metrology with spin qubits*. *Phys. Rev. A* **85**, 032336 (2012)
- [8] G. Goldstein, P. Cappellaro, J. R. Maze, J. S. Hodges, L. Jiang, A. S. Sørensen, and M. D. Lukin, *Environment-assisted precision measurement*. *Phys. Rev. Lett.* **106**, 140502 (2011)
- [9] L. P. McGuinness, Y. Yan, A. Stacey, D. A. Simpson, L. T. Hall, D. Maclaurin, S. Prawer, P. Mulvaney, J. Wrachtrup, F. Caruso, R. E. Scholten, and L. C. L. Hollenberg, *Quantum measurement and orientation tracking of fluorescent nanodiamonds inside living cells*. *Nature Nanotech.* **6**, 358–363 (2011)
- [10] N. F. Ramsey, *Molecular beams* (Oxford University Press, 1990)
- [11] E. L. Hahn, *Spin echoes*. *Phys. Rev.* **80**, 580–594 (1950)
- [12] S. Meiboom and D. Gill, *Modified spin-echo method for measuring nuclear relaxation times*. *Rev. Sc. Instr.* **29**, 688 (1958)
- [13] N. Kosugi, S. Matsuo, K. Konno, and N. Hatakenaka, *Theory of damped Rabi oscillations*. *Phys. Rev. B* **72**, 172509 (2005)
- [14] H. Fedder, F. Dolde, F. Rempp, T. Wolf, P. Hemmer, F. Jelezko, and J. Wrachtrup, *Towards T_1 -limited magnetic resonance imaging using Rabi beats*. *Appl. Phys. B* **102**, 497–502 (2011)
- [15] M. H. Levitt, *Composite pulses*. *Prog. Nucl. Mag. Res. Spect.* **18**, 61–122 (1986)
- [16] I. Solomon, *Multiple echoes in solids*. *Phys. Rev.* **110**, 61–65 (1958)
- [17] A. Laraoui and C. A. Meriles, *Rotating frame spin dynamics of a nitrogen-vacancy center in a diamond nanocrystal*. *Phys. Rev. B* **84**, 161403 (2011)
- [18] J.-M. Cai, B. Naydenov, R. Pfeiffer, L. P. McGuinness, K. D. Jahnke, F. Jelezko, M. B. Plenio, and A. Retzker, *Robust dynamical decoupling with concatenated continuous driving*. *New J. Phys.* **14**, 113023 (2012)
- [19] X. Xu, Z. Wang, C. Duan, P. Huang, P. Wang, Y. Wang, N. Xu, X. Kong, F. Shi, X. Rong, and J. Du, *Coherence-protected quantum gate by continuous dynamical decoupling in diamond*. *Phys. Rev. Lett.* **109**, 070502 (2012)
- [20] M. Hirose, C. D. Aiello, and P. Cappellaro, *Continuous dynamical decoupling magnetometry*. Preprint at <http://arXiv.org/abs/1207.5729> (2012)
- [21] U. Haeberlen, *High resolution NMR in solids: selective averaging* (Academic Press Inc., New York, 1976)
- [22] D. J. Wineland, J. J. Bollinger, W. M. Itano, F. L. Moore, and D. J. Heinzen, *Spin squeezing and reduced quantum noise in spectroscopy*. *Phys. Rev. A* **46**, R6797 (1992)
- [23] R. S. Schoenfeld and W. Harneit, *Real time magnetic field sensing and imaging using a single spin in diamond*. *Phys. Rev. Lett.* **106**, 030802 (2011)
- [24] A. Dréau, M. Lesik, L. Rondin, P. Spinicelli, O. Arcizet, J.-F. Roch, and V. Jacques, *Avoiding power broadening in optically detected magnetic resonance of single NV defects for enhanced DC magnetic field sensitivity*. *Phys. Rev. B* **84**, 195204 (2011)
- [25] G. Balasubramanian, P. Neumann, D. Twitchen, M. Markham, R. Kolesov, N. Mizuochi, J. Isoya, J. Achard, J. Beck, J. Tissler, V. Jacques, P. R. Hemmer, F. Jelezko, and J. Wrachtrup, *Ultralong spin coherence time in isotopically engineered diamond*. *Nature Mater.* **8**, 383–387 (2009)
- [26] T. M. Babinec, H. J. M., M. Khan, Y. Zhang, J. R. Maze, P. R. Hemmer, and M. Loncar, *A diamond nanowire single-photon source*. *Nature Nanotech.* **5**, 195–199 (2010)
- [27] P. Neumann, J. Beck, M. Steiner, F. Rempp, H. Fedder, P. R. Hemmer, J. Wrachtrup, and F. Jelezko, *Single-shot readout of a single nuclear spin*. *Science* **5991**, 542–544 (2010)
- [28] J. R. Klauder and P. W. Anderson, *Spectral diffusion decay in spin resonance experiments*. *Phys. Rev.* **125**, 912–932 (1962)
- [29] G. J. Augustine, F. Santamaria, and K. Tanaka, *Local calcium signaling in neurons*. *Neuron* **40**, 331–346 (2003)
- [30] D. X. Keller, K. M. Franks, T. M. Bartol Jr, and T. J. Sejnowski, *Calmodulin activation by calcium transients in the postsynaptic density of dendritic spines*. *PLoS ONE* **3**, e2045 (2008)
- [31] C. L. Degen, *Scanning magnetic field microscope with a diamond single-spin sensor*. *Appl. Phys. Lett.* **92**, 243111 (2008)

- [32] M. S. Grinolds, P. Maletinsky, S. Hong, M. D. Lukin, R. L. Walsworth, and A. Yacoby, *Quantum control of proximal spins using nanoscale magnetic resonance imaging*. [Nature Phys.](#) **7**, 687–692 (2011)
- [33] W. W. S. Wei, *Time series analysis: univariate and multivariate methods* (Pearson Addison Wesley, 2006)
- [34] V. Jacques, P. Neumann, J. Beck, M. Markham, D. Twitchen, J. Meijer, F. Kaiser, G. Balasubramanian, F. Jelezko, and J. Wrachtrup, *Dynamic Polarization of Single Nuclear Spins by Optical Pumping of Nitrogen-Vacancy Color Centers in Diamond at Room Temperature*. [Phys. Rev. Lett.](#) **102**, 057403 (2009)

ACKNOWLEDGEMENTS

C. D. A. thanks Boerge Hemmerling, Michael G. Schmidt and Marcos Coque Jr. for stimulating discussions. This work was supported in part by the U.S. Army Research Office through a MURI grant No. W911NF-11-1-0400 and by DARPA (QuASAR program). C. D. A. acknowledges support from the Schlumberger Foundation.

AUTHOR CONTRIBUTIONS

C. D. A., M. H. and P. C. conceived the experiment and performed the theoretical analysis. C. D. A. and M. H. carried out the measurements and analysis of the data. All authors discussed the results and contributed to the manuscript.

ADDITIONAL INFORMATION

The authors declare no competing financial interests. Supplementary information accompanies this paper.

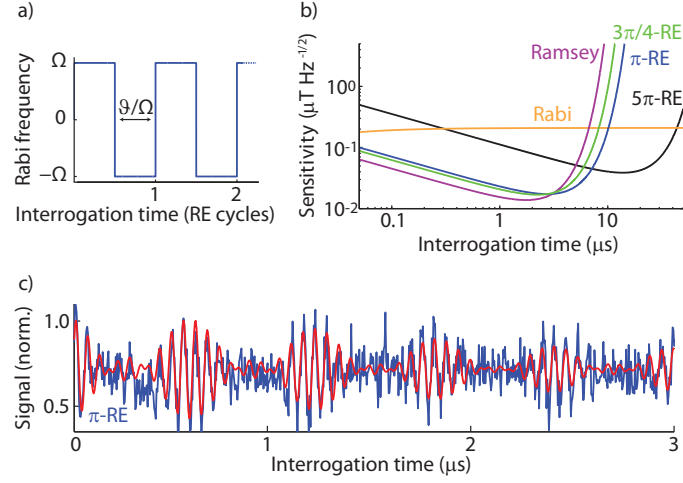


FIG. 1. Rotary-echo magnetometry scheme and expected sensitivity. a) Experimental control composed of a n -cycle ϑ -rotary-echo (RE) sequence, in which the phase of the microwave field is switched by π at every pulse of duration $\frac{\vartheta}{\Omega}$, where Ω is the Rabi frequency. b) Magnetometry sensitivities η_{RE} of $\vartheta = \{3\pi/4, \pi, 5\pi\}$ -RE sequences (green, blue, black), showing the tunability with the half-echo rotation angle. The sensitivity has its global minimum $\eta_{\text{RE}} \approx 1.38/\sqrt{t}$ (comparable to Ramsey magnetometry, purple) for $\vartheta \approx \frac{3\pi}{4}$ and consecutively increasing local minima for $\vartheta \approx (2k+1)\pi$. A decrease in sensitivity is followed by an increase in coherence time, which can approach T_1 as in Rabi-beat magnetometry (orange), whose sensitivity is limited by Ω . Sensitivities are simulated in the presence of static bath noise using parameters from the fit depicted in c). c) A typical normalized fluorescence signal after $n = 55$ RE cycles for $\vartheta = \pi$ and $\Omega \approx 2\pi \times 17\text{MHz}$ (blue); the modulation in the signal is due to the hyperfine interaction with the ^{14}N nucleus. The signal is filtered for even harmonics of $\pi\Omega/(\vartheta \bmod 2\pi)$ (Supplementary Methods, ‘Dynamics under rotary-echo sequence’) and then fitted to Eq. 1, modified to include decoherence induced by static bath noise (red).

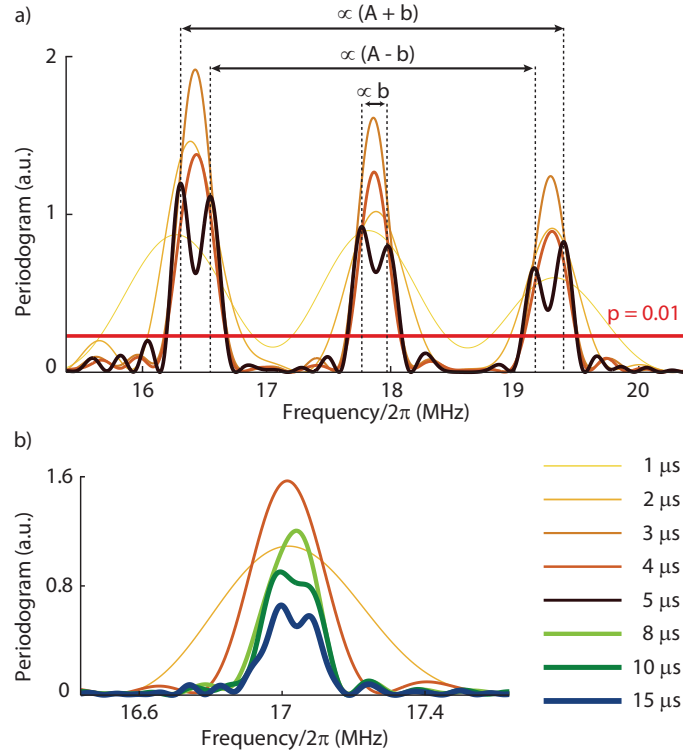


FIG. 2. **The periodogram identifies the frequency content of the signal.** a) Experimental periodogram for π -rotary-echo sequence for increasing interrogation times (thicker lines from 1 to $5\mu\text{s}$, in intervals of $1\mu\text{s}$). The periodogram is defined as the squared magnitude of the Fourier transform of the time signal. A pair of symmetric peaks about the Rabi frequency Ω signals the existence of one detuning $\delta\omega$. The number of resolved frequencies increases with time, at the expense of signal-to-noise ratio. After $5\mu\text{s}$ of interrogation, we can estimate both the hyperfine interaction $A \approx 2\pi \times (2.14 \pm 0.03)\text{MHz}$ and a small residual detuning from the presumed resonance, $b \approx 2\pi \times (0.17 \pm 0.02)\text{MHz}$. In this estimate, we correct for the real rotation angle $\vartheta \approx 0.96\pi$ using the difference between the nominal and experimentally realized Rabi frequency (symmetry point in the spectrum). The uncertainty in the measurement is estimated taking into account the total interrogation time, the number of points in the time-domain signal, and the S/N (Supplementary Methods, ‘Periodogram’). Periodogram peaks can be tested for their statistical significance [33] (also Supplementary Methods, ‘Periodogram’); we confirm that all 6 frequency peaks are considerably more significant than a $p = 0.01$ significance level (red). b) Innermost pair of frequency peaks arising from a $b \approx 2\pi \times (64 \pm 12)\text{kHz}$ residual detuning in another experimental realization, for an interrogation time of $15\mu\text{s}$.

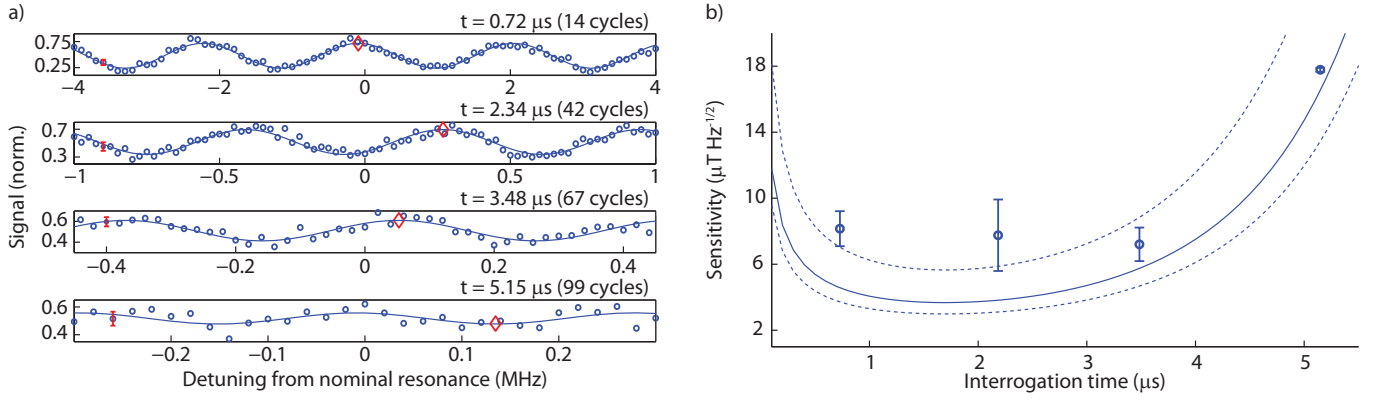


FIG. 3. **Experimental sensitivity of rotary-echo magnetometry.** a) Rotary-echo signals at fixed interrogation times, indicated on top of each sub panel, as a function of the detuning $\delta\omega$ from resonance. The signals are used to numerically calculate $|\frac{\partial S}{\partial \delta\omega}|$ and thus obtain the sensitivity η , given by Eq. 2. With increasing interrogation times, the slopes initially increase, indicating an improvement in η ; the effect of decoherence for the longer interrogation times degrades the sensitivity, and the slopes smoothen accordingly. The different amplitude modulations are due to the three-frequencies in the signal, $\{b, A \pm b\}$; polarizing the nuclear spin [34] would eliminate this modulation. From the fitted resonances for each curve (red diamonds), we estimate the true resonance to be at 0.09 ± 0.15 MHz from the presumed resonance. Typical standard deviations in the measurement are indicated (red error bars). Interrogation times are chosen to coincide with minima of the sensitivity in the presence of the hyperfine interaction; in other words, the correction factor C_A is at a local maximum at those times (Supplementary Methods, ‘Experimental sensitivity’, and Supplementary Fig. S3). b) For each fixed interrogation time, we plot the minimum sensitivity η within one oscillation period of the fitted oscillation frequency obtained in a), $\tau = 2t \sin(\vartheta/2)/\vartheta$ (Supplementary Methods, ‘Experimental sensitivity’, and Supplementary Fig. S4.a). The experimental points agree in trend with the theoretically expected sensitivities $\eta/(C \times C_A)$ (solid curves), here corrected for the presence of static bath noise, $\eta \rightarrow \eta e^{(t/T'_{\text{RE}})^2}$. T'_{RE} was computed using a $T_2^* \approx 2.19 \pm 0.15 \mu\text{s}$ fitting from a Ramsey decay experiment (Supplementary Fig. S4.b). The dashed blue lines indicate the lower (higher) bounds for the sensitivity estimated by dividing the theoretical sensitivity by the maximum (minimum) $C \times C_A$ value in the set of points. The standard deviation is shown in the error bar for each point.

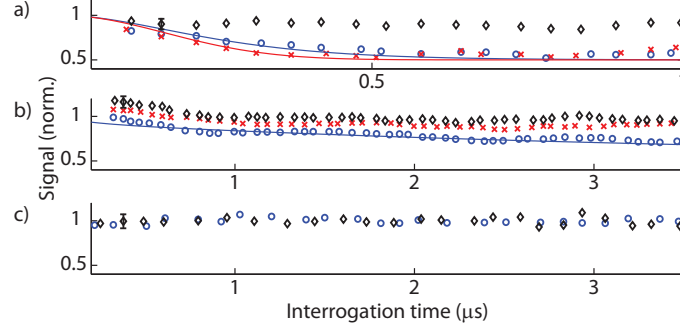


FIG. 4. **The rotary-echo is robust against added microwave frequency noise.** 40 realizations of both static (red) and Ornstein-Uhlenbeck (OU, $\tau_c = 200\text{ns}$, blue) microwave noise of strength 0.05Ω , where $\Omega \approx 2\pi \times 19\text{MHz}$ is the Rabi frequency, for a) Rabi, b) 5π -rotary-echo (RE) and c) π -RE sequences. We note that the correlation time of the driving field noise was purposely set much shorter than what usually observed in experiments in order to enhance the different behaviour of π -RE and 5π -RE. Typical standard deviations in the measurement are indicated (black error bars). a) We plot the peak of the Rabi fringes in the presence of static (red crosses) and OU (blue circles) microwave noise, which are in agreement with the expected theoretical decay (solid blue line and solid red line, respectively) (Supplementary Methods, ‘Evolution under excitation field noise’ and Supplementary Fig. 5.b). The oscillations at the tail of the signals are due to the finite number of experimental realizations. The peaks of a no-noise Rabi experiment are plotted for comparison (black diamonds). b) The peak of the 5π -RE revivals are plotted in the presence of static (red crosses) and OU (blue circles) microwave noise; the peaks of the 5π -RE in the absence of microwave noise are also plotted for comparison (black diamonds). Whereas the echo virtually does not decay in the presence of static noise, under the effect of stochastic noise, the echo decays only weakly as stipulated by theory (solid blue line) (Supplementary Methods, ‘Evolution under excitation field noise’ and Supplementary Fig. 5.b). c) The peak of the π -RE revivals are plotted in the presence of OU microwave noise (blue circles); virtually no decay is found if compared to the peaks of a no-noise experiment (black diamonds).